Microeconomics and Mechanism Design
Master 2
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1 Introduction

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3. The Gale-Shapley algorithm
    - The Deferred Acceptance algorithm
    - Optimal stable matchings
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5 References

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